

# **Exponential Growth**



x	0	1	2	3	4	5	6
y	1	2	4	8	16	32	64

Use the table above to find:

a.)  $f(4) = \underline{\hspace{2cm}}$       b.)  $f(0) = \underline{\hspace{2cm}}$       c.)  $f(2) = \underline{\hspace{2cm}}$       d.)  $f(5) = \underline{\hspace{2cm}}$

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Use the function rule to find the following:  $f(x) = 2^x$

a.)  $f(1) = \underline{\hspace{2cm}}$       b.)  $f(2) = \underline{\hspace{2cm}}$       c.)  $f(3) = \underline{\hspace{2cm}}$       d.)  $f(4) = \underline{\hspace{2cm}}$

Use the function rule to find the following:  $f(x) = 2(3)^x$

a.)  $f(1) = \underline{\hspace{2cm}}$       b.)  $f(2) = \underline{\hspace{2cm}}$       c.)  $f(3) = \underline{\hspace{2cm}}$       d.)  $f(4) = \underline{\hspace{2cm}}$

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Find the power

Use the function rule to find the following values of x:  $f(x) = 3^x$

a.)  $f(x) = 3$

$(x=1)$   $3^x = 3$

b.)  $f(x) = 81$

$3^x = 81$   $(x=4)$

c.)  $f(x) = 9$

$3^x = 9$   $(x=2)$

d.)  $f(x) = 27$

$3^x = 27$   $(x=3)$

Use the function rule to find the following:  $f(x) = 3(2)^x$

a.)  $f(x) = 6$

$\cancel{3}(2)^x = \frac{6}{\cancel{3}}$

$2^x = 2$

$(x=1)$

b.)  $f(x) = 48$

$\cancel{3}(2)^x = \frac{48}{\cancel{3}}$

$2^x = 16$

$(x=4)$

c.)  $f(x) = 12$

$\cancel{3}(2)^x = \frac{12}{\cancel{3}}$

$2^x = 4$

$(x=2)$

d.)  $f(x) = 24$

$\frac{3(2)}{3}(2)^x = \frac{24}{3}$

$2^x = 8$

$(x=3)$

## *Average Rate of Change (Exponential Functions)*

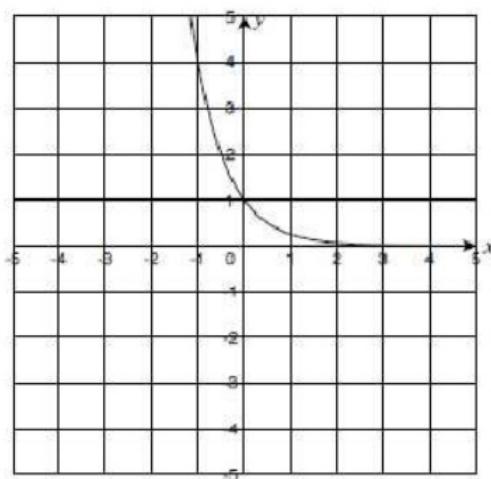
Find the average rate of change for the following functions over the given interval. What does the average rate of change tell you about the function on the interval?

a)

$x$	0	1	2	3	4
$f(x)$	3	6	12	24	48

From  $x = 0$  to  $x = 3$

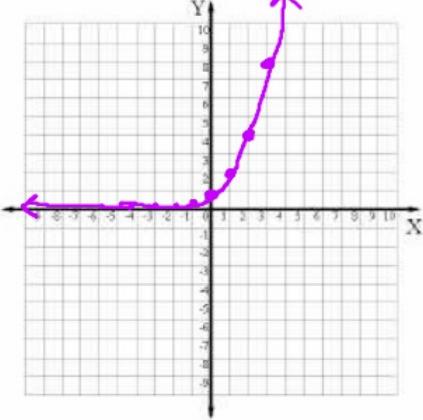
b)



From  $x = -1$  to  $x = 1$

c.  $y = 2^x + 1$  [2, 4]

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Main Ideas	Details																										
	<p>Using a graphing calculator, graph the function <math>f(x) = 2^x</math> and sketch the graph on the grid provided below.</p> <p><math>x \mid y = 2^x</math></p> <table border="1"><tr><td>3</td><td>8</td></tr><tr><td>2</td><td>4</td></tr><tr><td>1</td><td>2</td></tr><tr><td>0</td><td>1</td></tr><tr><td>-1</td><td>1/2</td></tr><tr><td>-2</td><td>1/4</td></tr><tr><td>-3</td><td>1/8</td></tr></table> <p></p> <p>1. Is the graph an increasing or decreasing function? Explain your answer. <i>Left to Right graph is Increasing</i></p> <p>2. Trace or use the table feature on your calculator to fill out the tables below. As the value of <u><math>x</math></u> gets very large, what happens to the value of <u><math>2^x</math></u>? <i>As x gets larger, <math>2^x</math> increase and gets larger</i></p> <table border="1"><tr><td>x</td><td><math>2^x</math></td></tr><tr><td>0</td><td>1</td></tr><tr><td>1</td><td>2</td></tr><tr><td>5</td><td>32</td></tr><tr><td>10</td><td>1024</td></tr><tr><td>20</td><td>1048576</td></tr></table>	3	8	2	4	1	2	0	1	-1	1/2	-2	1/4	-3	1/8	x	$2^x$	0	1	1	2	5	32	10	1024	20	1048576
3	8																										
2	4																										
1	2																										
0	1																										
-1	1/2																										
-2	1/4																										
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x	$2^x$																										
0	1																										
1	2																										
5	32																										
10	1024																										
20	1048576																										

As the value of  $x$  gets very small, what happens to the value of  $2^x$ ?

$x$	$2^x$
-1	1/2
-3	1/8
-5	1/32
-10	1/1024
-20	1/1,048,576

$2^x$  gets smaller,  
closer to zero, but  
never touches zero

3. Will the value of  $2^x$  ever equal 0? Explain your answer.

NO, because the numerator will never be 0

4. Are there any values of  $x$  that would make  $2^x$  undefined? Explain your answer.

NO, because positive  $x$ 's are large  
negative  $x$ 's are small  
 $x=0 \quad 2^x=1$

5. State the domain and range for  $f(x) = 2^x$ .

Left to Right

Domain:  $(-\infty, \infty)$

Bottom to Top

Range:  $(0, \infty)$